

Instructions: Write complete solutions to the following problems in the space provided. Be sure to supply all the necessary steps that lead to your answers

1. Consider the function $f(x, y) = xy^2$ Ans _____

a. Find $\int_0^1 f(x, y) dx$

b. Find $\int_1^2 f(x, y) dy$ Ans _____

2. Evaluate the double integral Ans _____

$$\int_0^2 \int_0^2 (xy^2 + yx^2) dx dy$$

3. Evaluate the double integral. Ans _____

$$\int_1^3 \int_2^4 \left(\frac{x}{y} + \frac{y}{x} \right) dx dy$$

4. Evaluate $\int_1^2 \int_0^1 2xy\sqrt{x^2 + y^2} dx dy$

Ans _____

5. Find the volume of the solid that lies under the elliptic paraboloid and above the rectangle

Ans _____

$$\frac{x^2}{9} + \frac{y^2}{16} + z = 1, \quad \mathfrak{R} : [-1, 1] \times [-2, 2]$$

6. Find the average value of f over the given rectangle

Ans _____

$$f(x, y) = 4x^2y, \quad \mathfrak{R} \text{ has the vertices } (-1, 0), (-1, 4), (1, 4), (1, 0).$$